Quantitative Techniques and Operations Research



SULTAN CHAND & SONS

Quantitative Techniques & Operations Research

Dr. S P GUPTA

Management Consultant
Formerly Head & Dean, Faculty of Management Studies
University of Delhi, Delhi

Dr. P K GUPTA

Associate Professor/Reader (Rtd.), J V Jain College, Saharanpur Formerly visiting faculty member, Department of Mathematics Cochin University of Science and Technology, Kochi



SULTAN CHAND & SONS

Educational Publishers
New Delhi

SULTAN CHAND & SONS

23, Daryagani, New Delhi-110002

Tel.: 23266105, 23277843, 23247051, 23243183, 23281876

E-mail: sultanchand74@yahoo.com; info@sultanchandandsons.com

Website: www.sultanchandandsons.com

First Edition: 2005

Third Edition: 2013, Reprint 2015, 2017, 2018, 2019

Fourth Revised Edition, 2022

ISBN: 978-93-5161-182-0 (TC-1017)

Price: ₹ 495.00

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Author's Acknowledgement: The writing of a Textbook always involves creation of a huge debt towards innumerable author's and publications. We owe our gratitude to all of them. We acknowledge our indebtedness in extensive footnotes throughout the book. If, for any reason, any acknowledgement has been left out we beg to be excused. We assure to carry out correction in the subsequent edition, as and when it is known.

Printed at: Sanjay Printers, Shahibabad, U.P.

Preface

This book has been designed primarily for BBA students of GGS Indraprastha University, NEW DELHI and other similar undergraduate courses in quantitative techniques of other universities.

Salient Features:

- The book covers syllabus of Quantitative Techniques & Operations Research paper of BBA completely. The students need to buy only one book instead of separate books on Statistics and Operations Research.
- There are detailed self-contained chapters on all the syllabus elements and are divided into two parts. Part I deals with the statistical techniques and Part II gives the operations research techniques.
- Part I of the book starts with chapter 0 giving meaning, classification of quantitative techniqes, its role in business and industry, and applications to real life problems. Chapter 1 deals with the meaning, uses, functions and limitations of statistics. Chapter 2 onwards discusses the classification of data, measures of Central Tendency, measures of Variation, Correlation, and Regression analysis.
- Part II starts with chapter 1 giving definition, modelling, methodology, applications and scope of operations research. Chapter 2 introduces the concept of linear programming and then familiarize the students with the Formulation of linear programming models. Methods for solving the linear programming problems, duality, transportation, and assignment problems that cover comprehensively the syllabus are discussed in chapter 2 through 6. Managerial applications are discussed at length.
- Chapter 7 on "Operations Scheduling" has been dealt with at greater length owing to its increasing importance in the current business environment.
- The language is simple and subject matter has been presented in a lucid and straight forward style and is self-explanatory. Special care has been taken to develop the concepts in a easy to understand manner.
- A sufficient number of solved examples and illustrations are given in each chapter to explain the various techniques of Statistics and Operations Research.
- Unsolved questions are given in the form of exercises followed by their answers for self practice.
- At the end of each chapter, conceptual questions in the form of "Test Your Understanding" and "Multiple - choice Questions" have been presented. These are followed by "Review Exercise" based on the theoretical questions dealt within the chapter.

Authors are grateful to Dr. Priyanshu Gupta, Assistant Professor, Indian Institute of Management, Lucknow for his valuable suggestions during revision of the book.

It is our firm belief that the book in its present form will be found most helpful by the undergraduate students of BBA and other similar courses.

Suggestions for improvement shall be gratefully received and duly acknowledged.

October 25, 2021 AUTHORS

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Syllabus

G.G.S. Indraprastha University B.B.A.—Second Semester

QUANTITATIVE TECHNIQUES & OPERATIONS RESEARCH IN MANAGEMENT

Contents

Unit I Lectures: 14

Statistics: Definition, Importance & Limitations. Collection of data and formation of frequency distribution. Graphic presentation of frequency distribution—Graphics, Bars, Histograms, Diagrammatic. Measures of central tendency—mean, median and mode. Partition values—quartiles, deciles and percentiles. Measures of variation—range, IQR, quartile deviation and standard deviation and Lorenz Curve.

Unit II Lectures: 10

Correlation Analysis: Correlation Coefficient; Assumptions of correlation analysis; Coefficients of determination and correlation; Measurement of correlation—Karl Pearson's Methods; Spearman's rank correlation; Concurrent deviation of the correlation coefficient; Pitfalls and limitations associated with regression and correlation analysis; real world application using IT tools.

Unit III Lectures: 14

Linear Programming: Concept and assumptions, usage in business decision-making, Linear programming problem: formulation. Methods of solving: Graphical and Simplex, problems with mixed constraints. Duality: Concept, significance, usage and application in business decision-making.

Unit IV Lectures: 14

Transportation and Assignment Problems: General structure of Transportation Problem, Different type of methods for finding Initial Solution by North-West Corner Rule, Least Cost Method and Vogel Approximation Method, and Testing for Optimality; Assignment Problem: Different Methods; Operations Scheduling: Scheduling Problems, Shop flow control, Gantt Charts, Principles of work center scheduling, Principles of Job Shop scheduling, Personnel scheduling.

About the Book

This book on Quantitative Techniques and Operations Research provides a conceptual understanding of basic quantitative techniques/methods used in solving managerial problems. It discusses comprehensively the essential topics of quantitative decision-making by using illustrations and examples. With revised and updated contents, this edition of the book will be useful to the students pursuing the undergraduate programme in Management and Commerce.

New in this Edition

- The chapters on Linear Programming Problems are rewritten and have been designed to take the reader through gradual increase in complexity. Chapter 2 of part II is completely dealt with the formulation of linear programming models from business and economics.
- Given its importance in the current business environment, chapter on Operations Scheduling has been dealt with at length.

About the Authors

Dr. S P Gupta (born 1942) has a brilliant academic record of teaching for more than 4 decades in Indian and Foreign Universities. He was a student of Shri Ram College of Commerce, University of Delhi. He obtained B.Com. (H) and M.Com. Degree with "Advanced Statistics" as specialization and taught for more than a decade in SRCC.

He was invited by the Tribhuvan University, Kathmandu, Nepal as visiting professor for a period of 2 years. He was also appointed visiting Professor in Karl Marx University, Milano for a period of 1 year. He attended prestigious International Teachers Program in Stockholm (Sweden) and Budapest, Hungary.



Dr. Gupta joined Faculty of Management Studies (FMS), University of Delhi from where he obtained Ph.D degree in Management and taught for about 3 decades. He has authored more than a dozen books in the field of Statistics for B.Com., M.Com., MBA, CA, ICWA courses etc. He was also Head & Dean, Faculty of Management Studies, University of Delhi for a period of 3 years.



Dr. P K Gupta has over three decades of experience in teaching Mathematics and Operations Research to undergraduate and Post-Graduate students. He obtained a master's degree in Mathematics, and then another one in Operations Research from the University of Delhi. He obtained his doctorate in 1977 in the field of Queuing Theory.

He served as a faculty member in various capacities at the Department of Mathematics, JV Jain College, Saharanpur; where he taught a range of topics on Mathematics and Operations Research. These included Boolean Algebra, Linear Algebra, Difference Equations, Graph Theory and Techniques of Operations Research.

In 1979, he was invited by the Cochin University of Science & Technology, Kochi (Kerala) to teach the students of their newly started diploma course in Operations Research and Computer Applications. He also has been actively engaged in research in the discipline. He supervised

multiple Ph.D. scholars in Optimization of Queues and also applied optimization techniques in paper industry. He has authored more than half a dozen books of Mathematics and Operations Research, in addition to multiple research publications.



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Phones : 011-23281876, 23277843, 23266105 Email : sultanchand74@yahoo.com

info@sultanchandandsons.com

Website: sultanchandandsons.com



